

# Inverse Design of Optimal Photonic Structures with Nonlinear Properties

**B. Allen,<sup>1</sup> Z. Lin,<sup>2</sup> A.W. Rodriguez<sup>2</sup>**

*1 – Washington University St. Louis*

*2 – Princeton University*

$$\nabla \times \frac{1}{\mu} \nabla \times \mathbf{E}(\mathbf{r}) - \omega^2 \epsilon(\mathbf{r}) \mathbf{E}(\mathbf{r}) = i\omega \mathbf{J}(\mathbf{r})$$

$$\mathbf{J}(\mathbf{r}, \mathbf{r}') = \hat{\mathbf{e}}_j \delta(\mathbf{r} - \mathbf{r}')$$

$$\text{Objective: } \text{Re} \left[ \int \mathbf{J}^* \cdot \mathbf{E} \, d\mathbf{r} \right]$$

Liang, X. D. and Johnson, S. G. Opt. Express 21(25) 30812 (2013)

## Linear Optics

- Induced polarization of material is linearly proportional to strength of the incident optical field
- $\mathbf{P} = \chi \mathbf{E}$

## Nonlinear Optics

- Induced polarization is proportional to some nonlinear combination

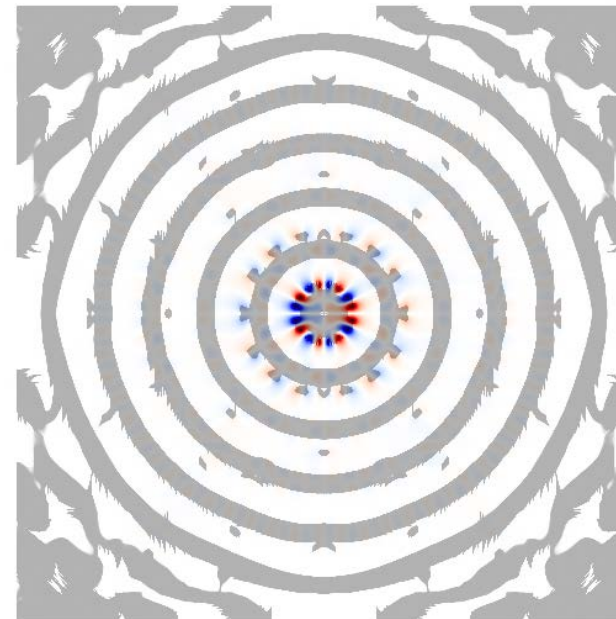
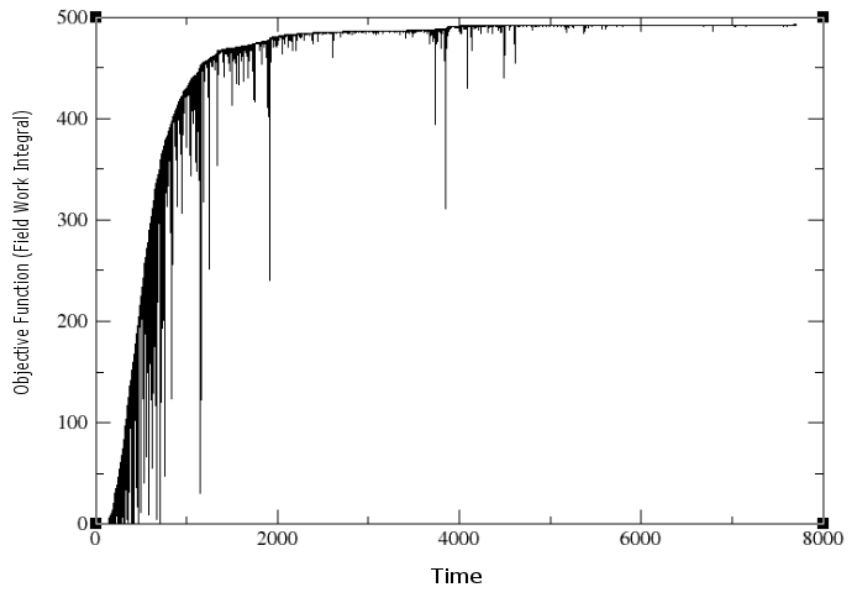
$$\mathbf{P} = \chi_1 \mathbf{E} + \chi_2 \mathbf{E} + \dots + \chi_n \mathbf{E}$$

- Nonlinear components represent harmonic generation within material

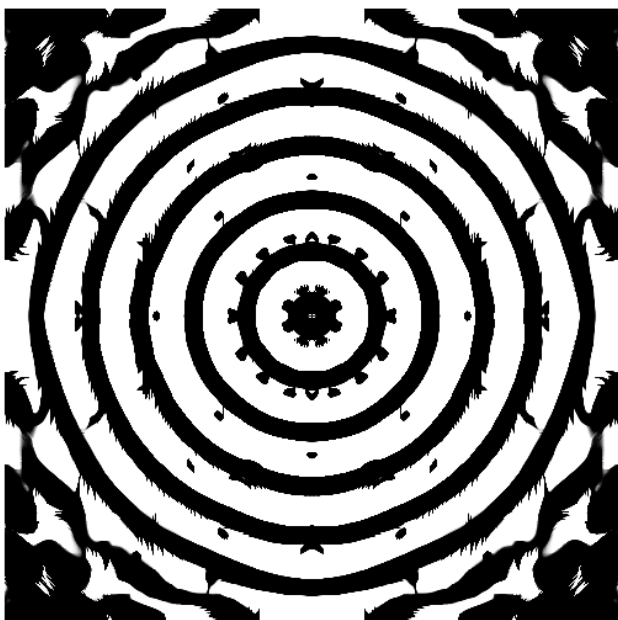
## Mode Confinement in Nonlinear Materials

- Structure must confine both  $\chi_1$  and  $\chi_n$  mode
- So-called “intuitive” structures typically only confine one mode
- De novo optimization enables design of structures capable of confining multiple modes

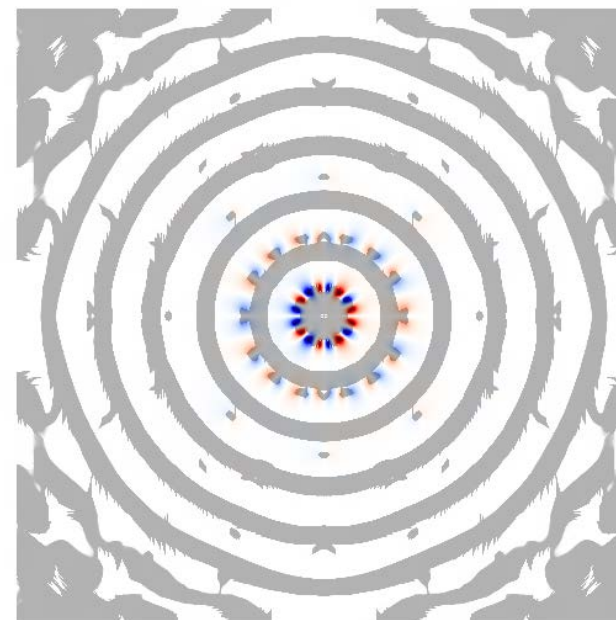
Field Work Integral vs. Time

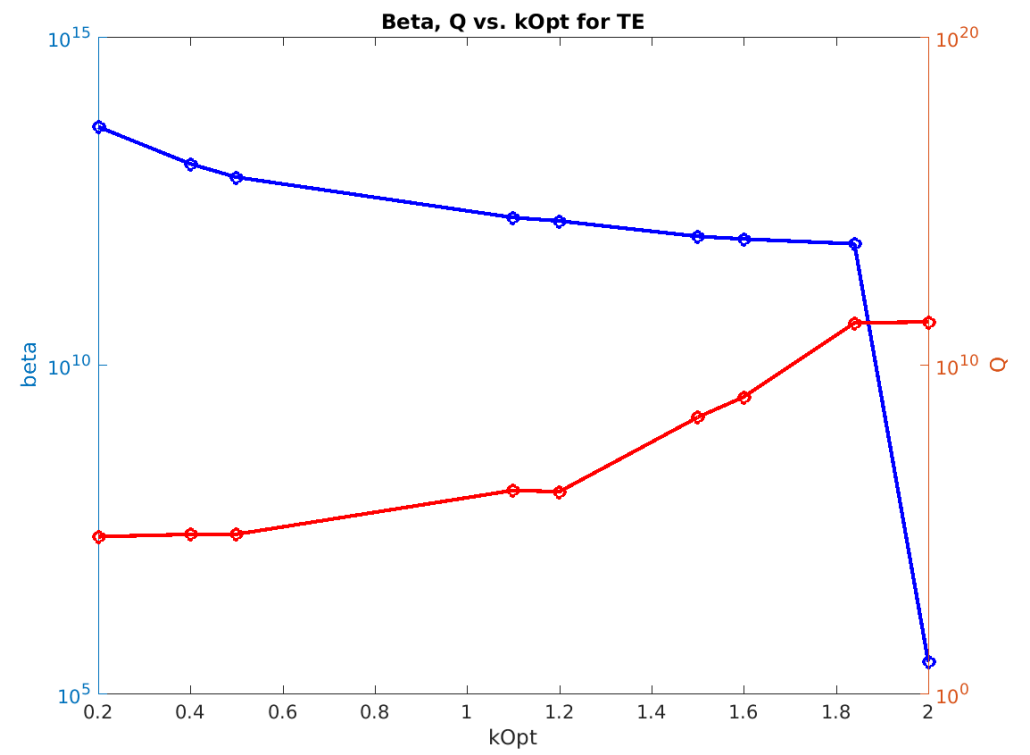
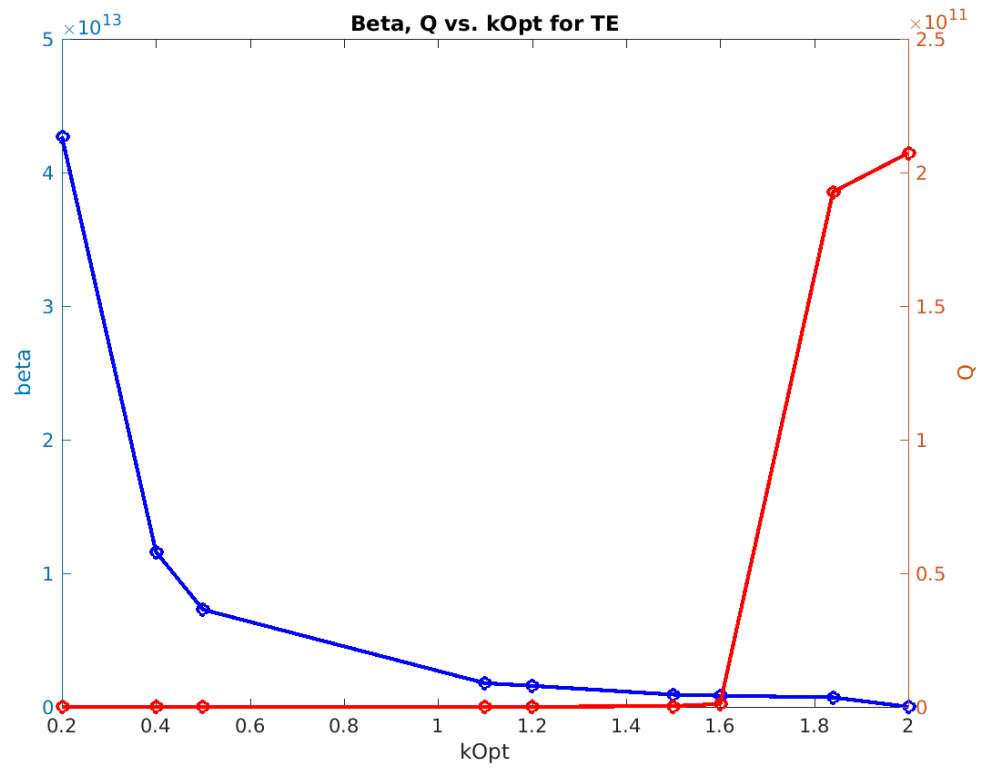


f1 mode



f3 mode





Figures of Merit